HBar Math Circle @ Walden Class 2 [2.27.2018]

[Problem 2.1] (20 min)

(i) How many squares are in the diagram below?

(ii) How about now?

(iii) How many rectangles are in the diagram below?

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(iv) [CHALLENGE] How about now?

[Problem 2.2] (20 min)

(i) List all the prime numbers that are less than 20.

- (ii) Is the number 324 prime? Why or why not?
- (iii) Is the number 1617 prime? Why or why not?

(iv) [CHALLENGE] Can you come up with a clever way to list all the prime numbers that are less than 100? What about 1000?

(v) [CHALLENGE] How many prime numbers are there? How do you know?

[Problem 2.3] (20 min)				
(i) Evaluate the nested fraction $\frac{1}{2/3}$				
(ii) Evaluate the nested fraction $\frac{1/2}{2/3}$				
(iii) [CHALLENGE] Evaluate the nested fraction $\frac{\frac{1}{2/3}}{3/9}$				
(iv) [CHALLENGE] Evaluate the nested fraction $\frac{\frac{1/2}{3/4}}{\frac{3/2}{3/4}}$				

[Problem 2.4] (30 min)

Let's play a game. You and your partner each pick a number between 1 and 100 and write it down on a sheet of paper without showing your partner. You put the paper face-down, and you and your partner try to guess each other's number. Each time you make a guess, your partner will tell you whether you got the number right, or if you didn't, then if your guess was too high or too low.

(i) Play a few rounds of the game.

(ii) What is the best strategy to win this game?

(iii) [CHALLENGE] Using this strategy, what is the largest number of guesses it could possibly take you to guess your partner's number?